

In general, a **Continued Fraction** is a fraction of the form $a_0 + \frac{b_0}{a_1 + \frac{b_1}{a_2 + \frac{b_2}{\dots + \frac{b_n}{a_n}}}}$ where $a_i, b_i \in \mathbb{Z}$ for $i \in \{1, \dots, n\}$.

For this talk, we will focus on cases where $b_i = 1$ for all i . If we allow our continued fraction to be infinite, we can represent any real number. Now, let's further consider the case where the a_i 's repeat or eventually repeat. A fraction of that form represents a quadratic irrational, or the root of a quadratic polynomial with integer coefficients. The goal of this talk is to learn about the intuition behind this claim, from a geometric point of view that is centered on the Farey Diagram, pictured below. If time permits, we will discuss the converse of this statement.

